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**Title:**  $s$ -numbers of elementary operators

**Abstract:** A well-known theorem of Fong and Sourour states that if  $E$  is an elementary operator acting on the space  $B(H)$  of all bounded linear operators on a Hilbert space  $H$  then  $E$  is compact if and only if it has the form  $E(X) = \sum_{i=1}^n A_i X B_i$ ,  $X \in B(H)$ , for some compact operators  $A_i$  and  $B_i$ ,  $i = 1, \dots, n$ . In this talk we provide versions of this result in the case the ideal of compact operators is replaced by an  $s$ -number ideal. More precisely, we relate the inclusion of an elementary operator  $E$  on  $B(H)$  in an  $s$ -number ideal in  $B(B(H))$  to the inclusion of the operators  $A_i$  and  $B_i$  in a suitable representation of  $E$  to the corresponding  $s$ -number ideal in  $B(H)$ . We pay special attention to the Hilbert, Kolmogorov and approximation  $s$ -number ideals. We give an  $s$ -number ideal version of a generalisation of the Fong-Sourour Theorem for prime  $C^*$ -algebras due to Mathieu.